UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
International General Certificate of Secondary Education

CANDIDATE
NAME

CENTRE
NUMBER

CANDIDATE
NUMBER

MATHEMATICS **0580/03, 0581/03**

Paper 3 (Core) **May/June 2009**

2 hours

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator   Geometrical instruments
                       Mathematical tables (optional)   Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a soft pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO **NOT** WRITE ON ANY BARCODES.

Answer **all** questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 104.

For Examiner's Use

This document consists of **16** printed pages.

UNIVERSITY *of* CAMBRIDGE
International Examinations

[Turn over

1 **(a)** Roberto owns 6000 square metres of land.
He divides it between himself and his two children, Stefano and Tania, in the ratio

Roberto : Stefano : Tania = 7 : 5 : 3.

(i) Show that Roberto now has 2800 square metres of land.
Answer(a)(i)

[2]

(ii) Calculate the area of land that Stefano and Tania each have.

Answer(a)(ii) Stefano .... m^2

Tania .... m^2 [2]

(b) Roberto receives a rent of $1.40 per month for each square metre of his land.

(i) Calculate the rent he receives in **one year** from his 2800 square metres of land.

Answer(b)(i) $ .... [2]

(ii) Roberto uses $\frac{3}{5}$ of this amount to buy more land.

Calculate the amount that he uses to buy more land.

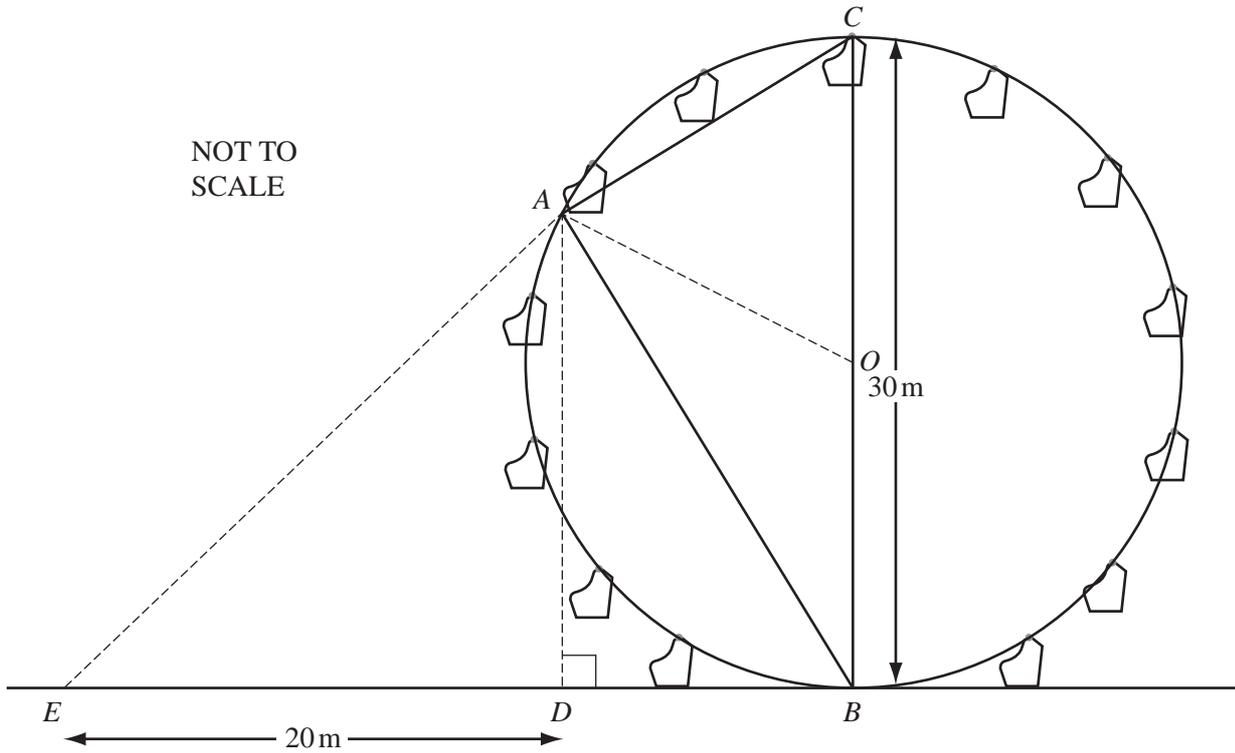*Answer(b)*(ii) $ .... [2]

For
iner's

(c) Stefano builds a house on his land.
He borrows $5000 from a bank at 8% per year **simple** interest.
Find the total amount of interest he will have paid at the end of 3 years.

Answer(c) $ .... [2]

(d) Tania sells her land for $12 000.
She invests the money for 3 years at 6% per year **compound** interest.
Calculate the total amount of money she will have at the end of the 3 years.
Give your answer to the nearest dollar.

Answer(d) $ .... [4]

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2   The diagram represents a fairground wheel with centre *O*, and diameter 30 metres.
     Point *D* is vertically below point *A*, and the line *EDB* is horizontal. *ED* = 20 metres.

NOT TO
SCALE

30 m

20 m

(a) A seat starts at *B* and travels one-third of the circumference to *A*.

Explain why angle *AOB* equals 120°.

Answer(a)

[1]

(b) Find the value, in degrees, of

   (i) angle *ABO*,

Answer(b)(i) Angle *ABO* = ... [1]

   (ii) angle *BAC*,

Answer(b)(ii) Angle *BAC* = ... [1]

   (iii) angle *ABD*.

Answer(b)(iii) Angle *ABD* = ... [1]

(c) (i) Use trigonometry in triangle *ABC* to calculate the distance *AB*.

Answer(c)(i) *AB* = ... m [2]

(ii) Show that *AD* = 22.5 metres.

Answer(c)(ii)

[2]

(d) Eshe holds her camera at *E* and takes a photograph of her friend in the seat at *A*.

Calculate angle *AED*.

Answer(d) .... [2]

3 **All the times given in this question are the local time in Paris.**

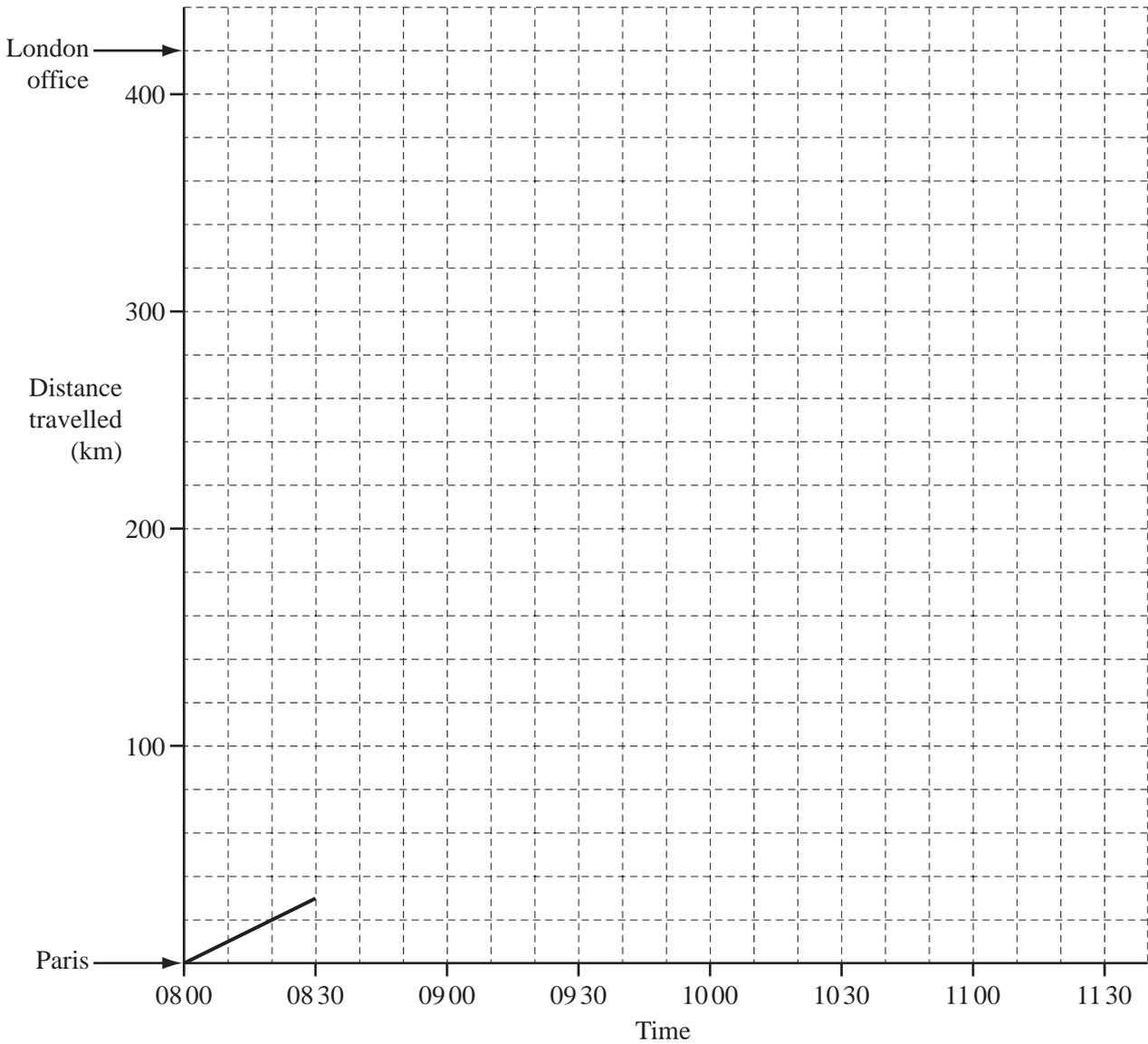Pierre left Paris at 08 00 to go to his office in London.
He travelled 30 kilometres to the airport.
He arrived at 08 30 and his plane left one hour later.
It flew 350 kilometres to London airport and landed at 10 15.
Pierre left London airport at 10 50 and he arrived at his office in London 40 minutes later.

(a) On the grid below, complete the travel graph.

London
office

400

300

Distance
travelled
(km)

200

100

Paris

08 00   08 30   09 00   09 30   10 00   10 30   11 00   11 30

Time

[4]

For
iner's

(b) (i) How long is the flight from Paris to London?
Give your answer in hours.

Answer(b)(i) .... h [1]

(ii) Calculate the average speed of the flight, in kilometres/hour.

Answer(b)(ii) .... km/h [2]

(c) Pierre's colleague, Annette, travelled from Paris to London by train.
She left at 09 50 and arrived at the London office at 12 45.
Calculate the difference in the times taken by Pierre and Annette for the whole journey.
Give your answer in minutes.

Answer(c) .... min [3]

For
iner's

4 **(a)** Garcia and Elena are each given x dollars.

(i) Elena spends 4 dollars.
Write down an expression in terms of x for the number of dollars she has now.

Answer(a)(i) $ .... [1]

(ii) Garcia doubles his money by working and then is given another 5 dollars.
Write down an expression in terms of x for the number of dollars he has now.

Answer(a)(ii) $ .... [1]

(iii) Garcia now has three times as much money as Elena.
Write down an equation in x to show this.

Answer(a)(iii) .... [1]

(iv) Solve the equation to find the value of x.

Answer(a)(iv) $x =$ .... [3]

(b) Solve the simultaneous equations

$$3x - 2y = 3,$$
$$x + 4y = 8.$$

Answer(b) $x =$ ....

$y =$ .... [3]

5
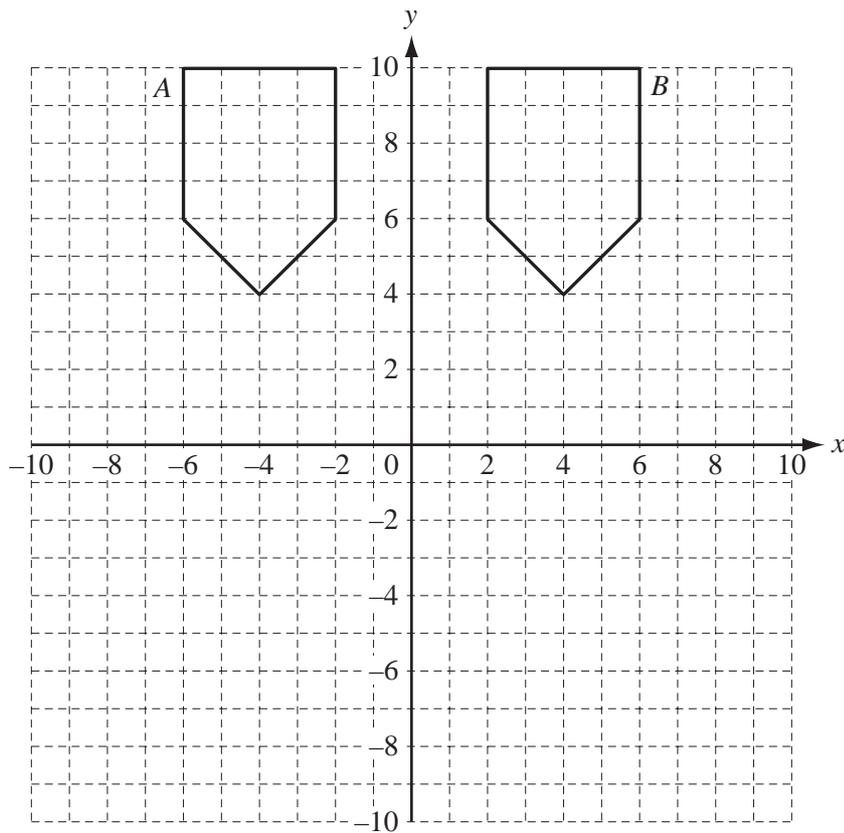
(a) Two different **single** transformations can map shape *A* onto shape *B*.

Describe each transformation fully.

Answer(a) ....

or .... [4]

(b) Reflect shape *A* in the *x* axis. Draw the image and label it *C*. [2]

(c) Rotate shape *B* through 90° clockwise about the origin. Draw the image and label it *D*. [2]

(d) Describe fully the **single** transformation which maps shape *C* onto shape *B*.

Answer(d) .... [3]

(e) Draw the enlargement of shape *A*, centre (−4, 8), with scale factor $\frac{1}{2}$.

Label the image *E*. [2]

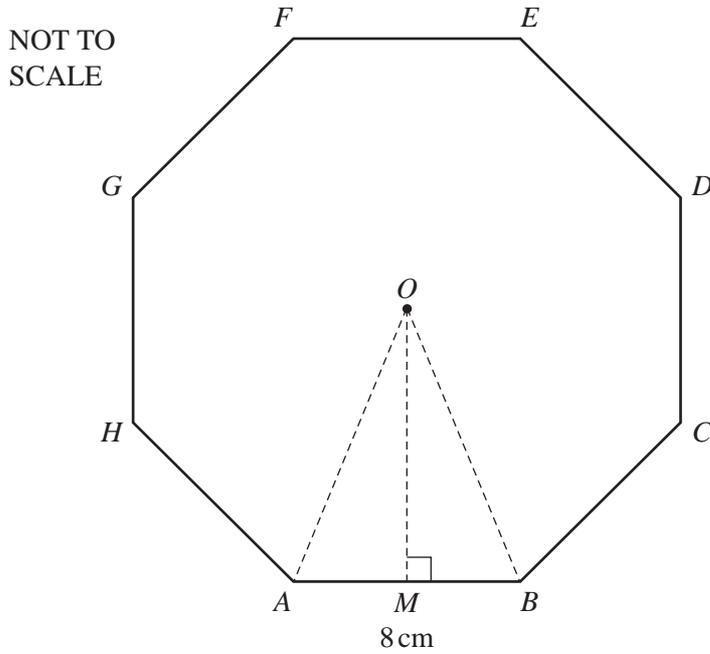**6** **(a)** Write down the name of a polygon with 8 sides.

Answer(a) .... [1]

(b) Find the size of the interior angle of a regular polygon with 8 sides.

Answer(b) .... [2]

(c) A regular 8-sided polygon, centre O, and side 8 cm, is shown below.
M is the mid-point of the side AB.

(i) Show that $OM = 9.66$ cm correct to 3 significant figures.

Answer (c)(i)

[3]

(ii) Calculate the area of the triangle *AOB*.

Answer(c)(ii) .... cm^2 [2]

(iii) Calculate the area of the polygon.

Answer(c)(iii) .... cm^2 [1]

(d) The polygon forms the cross-section of a box.
The box is a prism of height 12 cm.

Calculate the volume of the box.

Answer(d) .... cm^3 [1]

(e) The box contains 200 toffees in the shape of cuboids, 3 cm by 2 cm by 2 cm.

Calculate

(i) the total volume of the 200 toffees,

Answer(e)(i) .... cm^3 [2]

(ii) the percentage of the volume of the box **not** filled by the toffees.

Answer(e)(ii) .... % [3]

7

$$y = 9x - x^2.$$

(a) Complete the table of values for this equation.

x	0	1	2	3	4	5	6	7	8	9
y		8			20	20			8	0

[3]

(b) On the grid below, draw the graph of $y = 9x - x^2$ for $0 \leqslant x \leqslant 9$.

[4]

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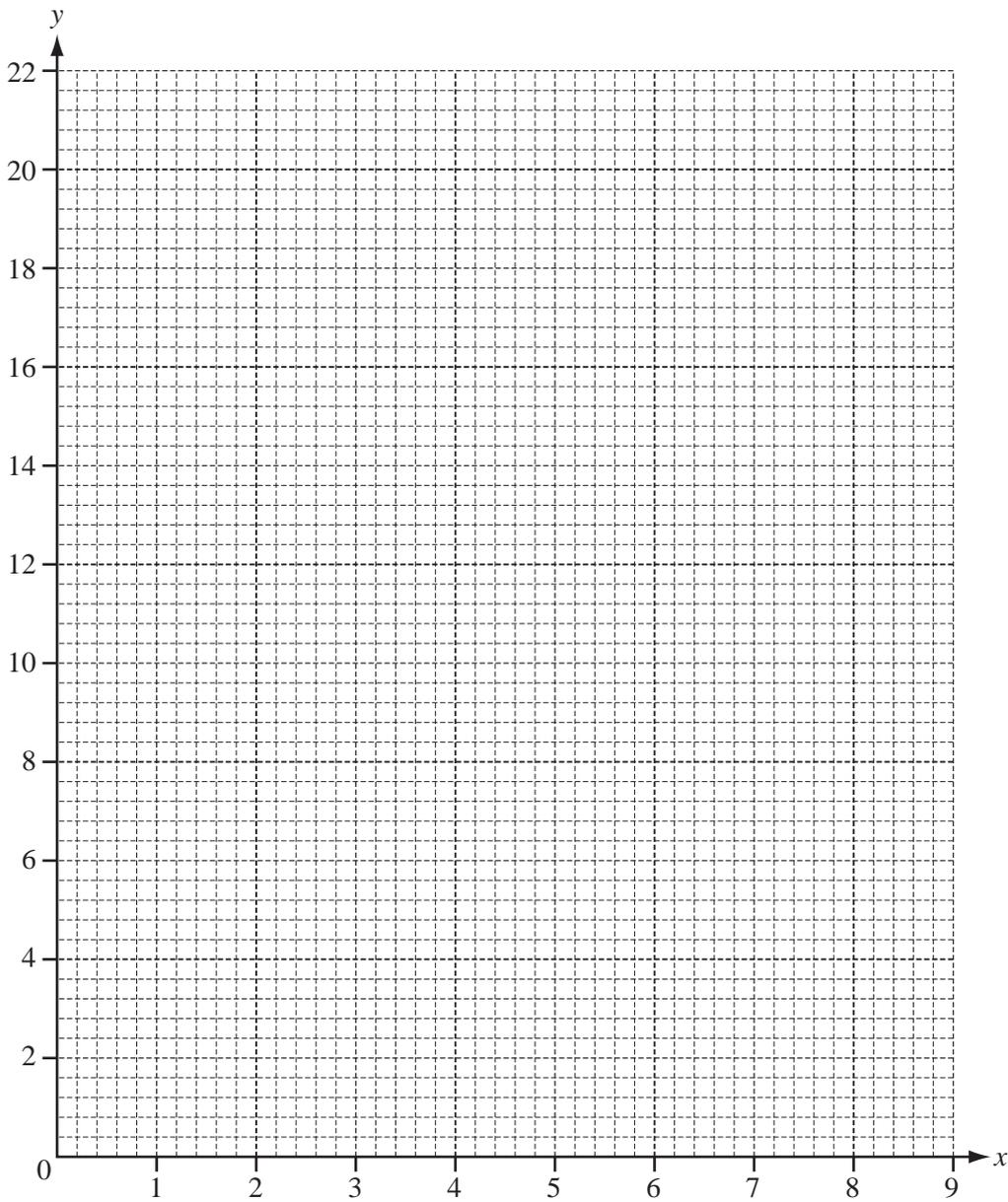
(c) Write down the values of x and y at the highest point of the curve.

Answer(c) $x =$ ....

$y =$ .... [2]

(d) (i) On the grid, draw the line $y = 6$ for $0 \leqslant x \leqslant 9$. [1]

(ii) Use this line to find the solutions of the equation

$$9x - x^2 = 6.$$

Give your answers correct to one decimal place.

Answer(d)(ii) $x =$ .... or $x =$ .... [2]

*For
~iner's*

8 The table below shows the age and price of 20 used cars in a showroom.

Age (years)	6	5	4	5	4	5	1	6	3	8
Price ($)	1800	7600	9500	2500	4100	3100	5600	4700	4800	7900
Age (years)	1	2	9	10	3	7	1	8	2	3
Price ($)	6500	7000	1000	3800	1900	5200	3400	2100	4300	8200

(a) Use this information to complete the following table.

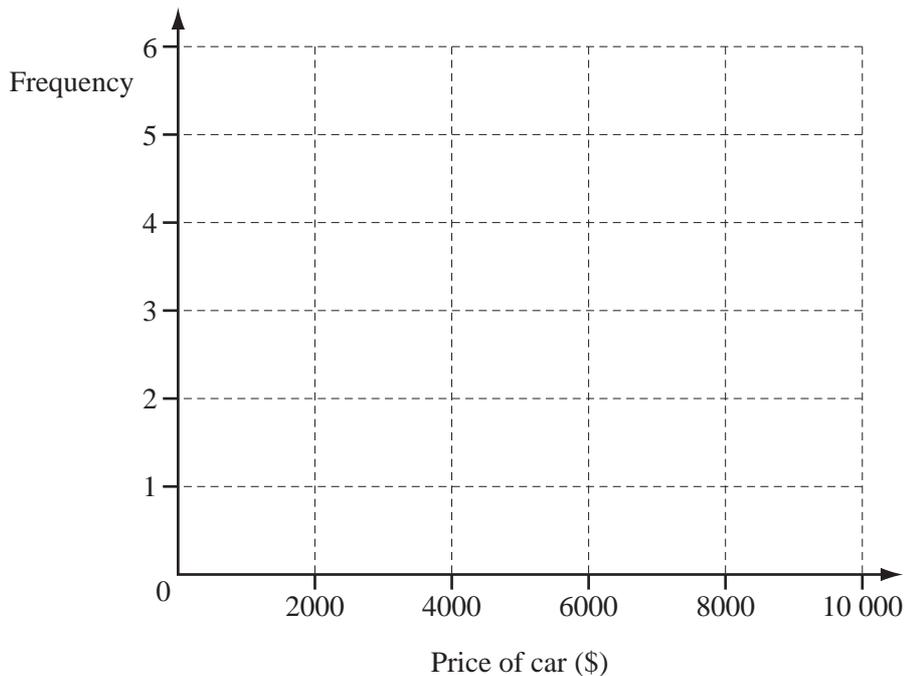| Age of cars (years)	Number of cars	Angle in a pie chart
1 to 3	8	144°
4 to 6	7	
7 or more		

[3]

(b) (i) Complete the frequency table for the price, $x, of the cars.

Price ($)	$0 \leqslant x < 2000$	$2000 \leqslant x < 4000$	$4000 \leqslant x < 6000$	$6000 \leqslant x < 8000$	$8000 \leqslant x < 10\,000$
Frequency					

[2]

(ii) Draw a histogram to show this information.

Frequency

Price of car ($)

[2]

(c) (i) On the grid below complete the scatter diagram showing the age and price of each car.

The first 10 points from the original table have been plotted.
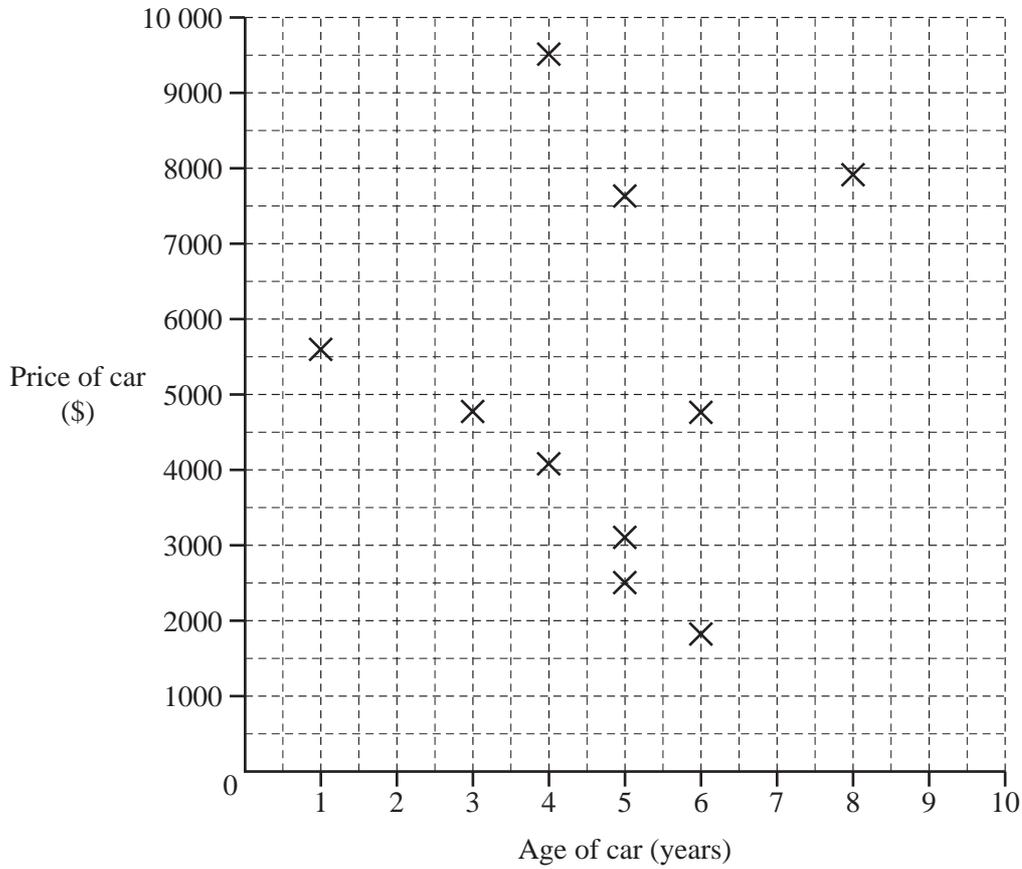
[3]

(ii) What correlation is there between the price of a car and its age?

Answer(c)(ii) .... [1]

(iii) A car is chosen at random.

Using your scatter diagram, find the probability that the car is more than 4 years old and the price is more than $5000.

Answer(c)(iii) .... [2]

Question 9 is on the next page

9 **(a)** The first four terms of a sequence are   12,   7,   2,   −3.

    (i) Write down the next two terms of the sequence.

Answer(a)(i) .... and .... [2]

    (ii) State the rule for finding the next term of the sequence.

Answer(a)(ii) .... [1]

    (iii) Write down an expression for the nth term of this sequence.

Answer(a)(iii) .... [2]

(b) The first four terms of another sequence are   −3,   2,   7,   12.

Write down an expression for the nth term of this sequence.

Answer(b) .... [2]

(c) Add together the expressions for the nth terms of both sequences.

Write your answer as simply as possible.

Answer(c) .... [1]